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# A Search Model of Experience Goods

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**Abstract.** We present a model in which consumers can learn about product varieties through search but cannot observe product quality before purchase. As search cost increases, search intensity and competition decrease, but the resulting higher price leads to higher return for quality investment and to more high-quality firms. The quality effect can dominate so that a higher search cost boosts both consumer and social welfare. In contrast, if product quality were observed before purchase, welfare would monotonically decrease in search cost. Our results show that the observability of product quality is an important determinant of how search frictions impact market performance.

**Keywords:** consumer search, experience goods, inspection goods, product quality, search cost

**JEL Classification Number:** D8, L1

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## 1. INTRODUCTION

Consumers often conduct costly search in order to find price and product information. The economics literature on consumer search, which is by now rather extensive, makes the standard assumption that product quality is uncovered from search: the products are “search” or “inspection” goods.<sup>1</sup> However, in many situations, although consumers can find price and product variety that match their needs through search, they are unable to observe product quality before purchase. For instance, consumers could be looking for a restaurant serving a certain type of food or a piece of furniture with a particular style, but the quality of the product—the meal or the furniture—is learned only after consumption. In this paper, we study search markets for such “experience” goods.

We present a model with both vertical and horizontal product differentiation. A firm’s product can be of either high or low quality, and consumers have heterogeneous match values for a high-quality product, with their value for a low-quality product normalized to zero. High- and low-quality products from the same firm have the same appearance, and the quality of the product is detected only after consumption.<sup>2</sup> Firms can also be of either high or low quality, with a high-quality firm being more likely to produce a high-quality product. (We thus draw a distinction between *firm* quality and *product* quality.) A consumer incurs a search cost in order to discover her match value for a firm’s product—knowing that the match value is materialized only if the product is of high quality—and its price.

We further assume that the market operates for two time periods. At the beginning of period 1, each firm can make an investment to permanently increase its quality—the prob-

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<sup>1</sup>Starting from the seminal work of Stigler (1961), the economics of consumer search has advanced in the directions of searching for low price among homogeneous sellers (e.g., Stahl, 1989) or for desired variety under horizontal differentiation (e.g., Wolinsky, 1986). More recent search models have considered vertical differentiation where, however, product quality is uncovered from search (see discussions later).

<sup>2</sup>This reflects the *experience* nature of the product. One natural interpretation is that a high-quality product has no defect, whereas a low-quality one contains a hidden defect that decreases the product’s value to the consumer. Products from different firms may have different “appearances” that reflect horizontal differentiation.

ability that its product is of high quality—with heterogeneous investment costs. Following purchases by the first-period consumers, firms may establish reputation about their quality to the next generation of consumers. In each period, once the set of active firms and their (average) quality is determined, they simultaneously choose prices, followed by consumer search across firms.

In formulating the model above, a concerted effort is made to ensure the model to be also readily applicable to the case of inspection goods: For inspection goods, a consumer would observe the quality of a firm’s product when searching it, and an inspection good is otherwise the same as an experience good in our model. This provides a unified framework that will allow us to illuminate how price and welfare in search markets depend on the observability of product quality.

We start with a preliminary analysis where the market has a given average firm quality. In addition to its intrinsic interest, this provides the basis for the analysis with endogenous firm quality. We show that there is a uniform-price equilibrium, where consumers conduct (random) sequential search with a reservation value. The equilibrium has interesting similarities and differences as compared to that for inspection goods. The reservation value is determined similarly as in models of search for horizontally differentiated products (e.g., Wolinsky, 1986), adjusting for the fact that here a match value is materialized only if the product is of high quality. Remarkably, this reservation value is the same for experience and inspection goods. However, whereas an increase in the average firm quality lowers equilibrium price for inspection goods, it tends to raise equilibrium price for experience goods: In both cases, more high-quality firms in the market will motivate consumers to search more intensively, leading to intensified price competition; but for experience goods it has the additional effect of making the demand for each firm less elastic, and under plausible conditions this demand effect dominates the competition effect.<sup>3</sup>

We next turn to the full analysis with endogenous firm quality and reputation. To capture the idea of firm reputation in a convenient way, we assume that (some) period-

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<sup>3</sup>As we shall show, despite the higher prices, an increase in the average firm quality in the market nevertheless will result in higher consumer and social welfare.

1 consumers will make public their product reviews that are observed by consumers in period 2, which enables the latter to infer a firm’s quality before search. Then, because consumers will have higher expected surplus by searching firms with higher (average) quality, in period 2 consumers will only search high-quality firms, even though they still cannot observe product quality before purchase. Thus, a high-quality firm will have a higher discounted sum of profits due to its reputation, which provides the incentive (return) for firms to improve quality early on.<sup>4</sup> In equilibrium, a firm will invest to become a high quality producer if and only if its investment cost realization does not exceed some cutoff value. This cutoff determines the average firm quality in period 1, and only high-quality firms will be active sellers in period 2. Consumer search and price competition in both periods are then determined similarly as in the benchmark case. What is most striking about the equilibrium is that search friction has non-monotonic impact on consumer and social welfare: they both first increase and eventually decrease in search cost. An increase in search cost lowers search intensity and competition—which we term as the search efficiency effect—under a given average firm quality, but the resulting higher price and profit increase the return to being a high quality firm, motivating more firms to invest in quality and leading to a higher average firm quality in period 1. We demonstrate that, under plausible conditions, the quality effect dominates the search efficiency effect when search cost is (sufficiently) low while the converse is true when search cost is relatively high.

Notably, in our model if consumers were able to observe product quality before purchase, then both consumer and social welfare would monotonically decrease in search cost, same as the familiar result from the existing literature. For inspection goods, a higher search cost also increases average firm quality in period 1 by boosting the return to reputation. Why, then, is the relationship between search cost and welfare sharply different for inspection and experience goods? As we illuminate through our analysis, when consumers can observe product quality before purchase, they can avoid the utility loss from a low-quality product by not purchasing it, and hence they do not gain from increases in (average) firm quality

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<sup>4</sup>In experience-goods markets, it is well recognized that reputation can furnish incentives for firms to provide high-quality products (e.g., Choi, 1998; Shapiro, 1983; Wernerfelt, 1988).

in the same way as they would when searching for experience goods. A higher search cost then always leads to lower welfare due to lower search efficiency.

We further compare the market provision of product quality with the social optimum. We show that equilibrium investment for quality is (socially) deficient when search cost is low, which is consistent with the result from the economics literature on experience goods where—without search frictions—firms typically invest too little in quality (e.g., Riordan, 1986; Shapiro, 1982). However, we also find that quality investment can be socially excessive when search cost is relatively high, contrary to the conventional wisdom. To understand the second part of the above result, notice that more high-quality firms will benefit consumers in period 1 but the higher total investment cost harms industry profit. When search cost is high, consumers tend to have low match values from search. They thus benefit less when higher firm quality increases the probability that the match values are materialized; but the private investment incentive is high due to the high profit from being a high-quality firm. The negative welfare effect of higher investment cost can thus dominate when search cost is high.

We finally extend our model to analyze the role of an intermediary, which can list sellers on its search platform by charging each of them a fixed fee and a percentage of its revenue. The intermediary can improve welfare by screening out low-quality sellers, especially when it can commit to a relatively small listing space on the platform and hence charge a high fixed fee to a listing seller. The high fixed fee deters the low-quality firms who are unable to earn repeat business, resulting in a separating equilibrium where only high-quality firms will be active in period 1 (and also in period 2). However, if the intermediary is unable to commit to a limited listing space on its search platform, then it is possible that both high- and low-quality firms will be active on the platform in period 1, but fewer firms will invest in quality because the intermediary's fee lowers the sellers' investment return. In this case, the intermediary reduces welfare.

To the best of our knowledge, ours is the first model of sequential search for experience goods. Wolinsky (1986) is an early contribution to the study of consumer search for horizontally differentiated products (for related contributions, see, e.g., Anderson and Renault,

1999; Armstrong et al., 2009; Haan and Moraga-González, 2011; Rhodes, 2011). Recent papers have analyzed consumer search across vertically-differentiated firms (e.g., Athey and Ellison, 2011; Chen and He, 2011), under both horizontal and vertical differentiation (e.g., Eliaz and Spiegler, 2011; Bar-Isaac et al., 2012; Chen and Zhang, 2018), or with investment in product quality (e.g., Fishman and Levy, 2015; Moraga-González and Sun, 2019)<sup>5</sup>. All of these and other studies on consumer search assume that product quality is known before consumers make purchases. Our model advances the literature in an important new direction, and our results provide new perspectives on how search frictions impact market performance.

The Internet, together with new information technology, has drastically reduced search cost for many products. In the existing consumer search literature, reductions in search cost generally benefit consumers and increase social welfare. This is true even when a lower search cost sometimes leads to higher market prices (e.g., Chen and Zhang, 2011; Bar-Isaac et al., 2012; Zhou, 2014; Moraga-González, et al., 2017; Choi, et al., 2018), or when it lowers product quality (e.g., Fishman and Levy, 2015; Moraga-González and Sun, 2019). Our model also suggests that there are important consumer and efficiency benefits from reducing search frictions, but it cautions that for experience goods, (further) decreases in search cost can actually reduce consumer and social welfare.<sup>6</sup> In fact, in our model the presence of some search friction is *necessary* in order for either consumer or social welfare to be maximized.<sup>7</sup>

In the rest of the paper, we describe our model in section 2, analyze the benchmark under a given average firm quality in section 3, and conduct the analysis with endogenous firm quality and reputation in section 4. We extend the model to include a search intermediary

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<sup>5</sup>Relatedly, Wolinsky (2005) and Moraga-González and Sun (2018) study consumer search models in which sellers exert costly efforts to create service plans.

<sup>6</sup>Taylor (2017) considers a model in which a seller can manipulate the browsing cost (search cost) of potential buyers. He shows that a higher browsing cost, by driving away less serious buyers and increasing the sales effort of the seller, can benefit consumers and increase welfare.

<sup>7</sup>This has an interesting connection to the result in Grossman and Stiglitz (1981) on the impossibility of the informationally efficient markets, even though our model and mechanism are very different from theirs.

in section 5, and conclude in section 6. Proofs are gathered in the appendix.

## 2. THE MODEL

The market contains a unit mass of firms and operates for two periods, 1 and 2. A firm's product quality,  $q$ , can be either high ( $H$ ) or low ( $L$ ). The probability that a firm's product is of high or low quality is respectively  $\beta$  and  $1-\beta$ , where  $\beta \in \{\beta_h, \beta_l\}$  and  $0 \leq \beta_l < \beta_h \leq 1$ .<sup>8</sup> Initially, all firms have  $\beta = \beta_l$ ; but at the beginning of period 1, each firm can privately make a one-time investment that costs  $x$ , to permanently increase its quality from  $\beta_l$  to  $\beta_h$ , where  $x$  is a privately-observed random draw from distribution  $G(x)$ , with density  $g(x) > 0$  on  $[0, \bar{x}]$  for some  $\bar{x} \in (0, \infty)$ . Each firm's quality ( $\beta$ ) is then determined and remains as the firm's private information. Production cost is normalized to zero.

In each period, a distinct unit mass of consumers are present in the market.<sup>9</sup> Each consumer desires to purchase one unit of the product. A consumer's valuation of an  $H$  product is  $u$ , which is a random draw from cumulative distribution function  $F(u)$ , and her valuation of an  $L$  product is normalized to zero. That is, a consumer's utility from a product is

$$\Gamma(q) = \begin{cases} u & \text{if } q = H \\ 0 & \text{if } q = L \end{cases}.$$

Hence, firms are differentiated both horizontally and vertically, respectively because each consumer's  $u$  is independently drawn across firms and because a high-quality firm ( $\beta = \beta_h$ ) is more likely to produce a high-quality product ( $q = H$ ). We assume that  $F(u)$  has corresponding density  $f(u) > 0$  on  $[0, \bar{u}]$ , with  $0 < \bar{u} < \infty$ .

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<sup>8</sup>Thus,  $\beta_h$  and  $\beta_l$  correspond to a high- and a low-quality firm, respectively. Our model nests the case where a high-quality firm only produces  $q = H$  while a low-quality firm only produces  $q = L$ , with  $\beta_h = 1$  and  $\beta_l = 0$ . We allow more general values of  $\beta_h$  and  $\beta_l$  so that there can be quality uncertainty for both types of firms.

<sup>9</sup>Each consumer thus purchases only once by assumption. We can extend the analysis to situations where (some) consumers may purchase in both periods, but this would complicate analysis because a consumer's search strategy would then depend on her likelihood of repeat purchases (from the same firm). Our assumption allows us to focus on how the experience nature of goods impacts consumer search.



To focus on experience goods, we assume that an  $H$  product and an  $L$  product from the same firm have the same appearance. By searching a firm, a consumer learns her  $u$  for the firm's product and the firm's price; she knows that her utility from the product is  $u$  only if  $q = H$  and she will observe  $q$  only after purchase, consuming the good in the same period. Each search costs the consumer  $s > 0$ . In each period, firms simultaneously and independently choose prices, after which consumers may conduct sequential search and make purchases. To capture the idea that firms can establish quality reputation, we assume that consumers of period 1 will furnish product reviews about whether  $q = H$  or  $L$  for each firm's product.<sup>10</sup> In period 2, a new cohort of consumers, who replace the first-period consumers, can observe these product reviews before conducting search. All values in period 2, when discounted to period 1, have a common discount factor  $\delta > 0$ .<sup>11</sup>

A firm's strategy specifies its investment decision based on its investment cost  $x$  and its prices  $p_1$  and  $p_2$  (possibly contingent on its  $\beta$ ) in the two periods. A period-1 consumer's strategy specifies her search and purchase decisions, whereas period-2 consumers may base these decisions also on observed product reviews. At a perfect Bayesian equilibrium, each firm's strategy maximizes its discounted sum of profit, holding beliefs about other firms' and consumers' strategies; each consumer's strategy maximizes her surplus (at any point of her sequential decision process), holding beliefs about firms' qualities and prices; and beliefs are consistent with strategies along the equilibrium path.

One desirable feature of our model is that it can be readily adapted to the study of "inspection goods"; in fact, if consumers were able to observe product quality ( $q$ ) when searching the firm, our model would become one of search for inspection goods. In the case of inspection goods, we may interpret  $\beta$  as the probability that the firm's product meets each consumer's needs, so that a higher quality firm—whose product possibly has broader appeal to consumers—has a higher  $\beta$ , as in Chen and He (2011). Our formulation allows

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<sup>10</sup>Our analysis will be the same whether all period-1 consumers or a randomly-drawn portion of them will publically reveal their product experiences. For ease of exposition, we assume all of them will.

<sup>11</sup>We may consider period 2 as combining all possible future periods after period 1 for which firms have established quality reputation, in which case  $\delta$  could be higher than 1.

us to compare results for experience and inspection goods in a unified framework, and to clarify how product quality observability matters for the functioning of search markets.

We analyze our model in two steps. First, as a benchmark, we study in section 3 consumer search and price competition in a single period of our model in which given portions of  $G$  and  $1 - G$  firms respectively have  $\beta = \beta_h$  and  $\beta = \beta_l$ , for  $G \in [0, 1]$ . This analysis has its independent interest, and it will provide the basis for the full analysis of our model with endogenous  $G$  and with two periods in section 4.

### 3. SEARCH AND PRICE UNDER GIVEN AVERAGE FIRM QUALITY

Consider a single period of our model, in which a given  $G \in [0, 1]$  portion of firms have  $\beta = \beta_h$ . The average firm quality in the market is then given as:

$$\gamma = G\beta_h + (1 - G)\beta_l. \quad (1)$$

For given  $\gamma$ , we first consider consumers' search strategy. As in search models for inspection goods in which firms are horizontally and vertically differentiated (e.g., Eliaz and Spiegler, 2011; Chen and Zhang, 2018), we focus on a uniform-price equilibrium where all firms charge the same price  $p_\gamma$ , and we shall discuss the motivation for this equilibrium when characterizing  $p_\gamma$  later. Each consumer's equilibrium search strategy, holding belief  $p_\gamma$ , solves the following dynamic search problem:

$$V_\gamma = \max_{u_\gamma} \left\{ -s + [1 - F(u_\gamma)] \frac{\int_{u_\gamma}^{\bar{u}} (\gamma u - p_\gamma) f(u) du}{[1 - F(u_\gamma)]} + F(u_\gamma) V_\gamma \right\}, \quad (2)$$

where  $V_\gamma$  is a consumer's (maximized) continuation value from searching a randomly-selected firm whose expected quality and price are respectively  $\gamma$  and  $p_\gamma$ . The consumer will sequentially and randomly search sellers, and will purchase when she finds a seller whose product value  $u$  reaches her optimal reservation value  $u_\gamma$  (provided the seller's price is indeed  $p_\gamma$ ). Each search costs  $s$ ; and under reservation value  $u_\gamma$ , the search will lead to a purchase with probability  $[1 - F(u_\gamma)]$  while the consumer will search again to receive continuation value  $V_\gamma$  with probability  $F(u_\gamma)$ . The consumer's optimal reservation value

$u_\gamma$  thus satisfies the first-order condition:

$$-(\gamma u_\gamma - p_\gamma) f(u_\gamma) + f(u_\gamma) V_\gamma = 0.$$

It follows that the consumer's continuation value, which is also the surplus for a consumer to engage in search or to participate in the market, is

$$V_\gamma = \gamma u_\gamma - p_\gamma, \tag{3}$$

and in equilibrium  $V_\gamma \geq 0$  to ensure consumers' participation in the market. Combining (2) and (3), we obtain

$$s = -[1 - F(u_\gamma)] V_\gamma + \int_{u_\gamma}^{\bar{u}} (\gamma u - p_\gamma) f(u) du,$$

which can be re-stated as the following condition for the optimal reservation value in search:

$$\gamma \int_{u_\gamma}^{\bar{u}} (u - u_\gamma) f(u) du = s. \tag{4}$$

The left-hand side of equation (4) is the consumer's expected benefit from one more search when she is currently at a seller with  $u_\gamma$ , which decreases in  $u_\gamma$ , while  $s$  is the marginal cost of the extra search. The condition extends the optimal search rule for horizontally differentiated products (e.g., Wolinsky, 1986), which is a special case of equation (4) when  $\gamma = 1$ . As we clarify shortly, when  $s < \bar{s}$ —which we shall assume—for some positive number  $\bar{s}$ , there exists a unique  $u_\gamma \in (0, \bar{u})$  that solves (4) and indeed  $V_\gamma > 0$ .

Consider next the pricing strategy by firms. At the proposed uniform-price equilibrium, consumers will have reservation value  $u_\gamma$  at any firm she searches that charges price  $p_\gamma$ , holding the equilibrium belief that all firms have expected quality  $\gamma$  and price  $p_\gamma$ . Now suppose that a firm deviates to a price  $p$ . The consumer's purchase decision at this firm will partly depend on her belief about the firm's  $\beta$ , as well as on her belief about other firms' prices and qualities following the deviation. The concept of perfect Bayesian equilibrium, which we adopt, does not constrain beliefs off the equilibrium path, potentially resulting in multiple equilibria. To overcome this well-known difficulty in dynamic games of imperfect information, we assume that consumers hold “passive belief” off the equilibrium path: at

the deviating firm with price  $p$ , each consumer believes that (i) the firm deviating to price  $p$  continues to have the expected quality  $\gamma$ , and (ii) any other firm continues to charge price  $p_\gamma$  with expected quality  $\gamma$ .

Part (ii) of the passive belief follows from the standard assumption in consumer search for differentiated products (e.g., Wolinsky, 1986), where following the deviation by one firm the other firms are expected to continue with the equilibrium price; and the expected quality of any such firm would then continue to be  $\gamma$ .<sup>12</sup> Part (i) of the assumption is motivated by the following consideration. In our model, if a price deviation is profitable for one  $\beta$  type, it must be equally profitable for the other  $\beta$  type. Thus, if the consumer believes the expected quality of the deviating firm to be, say,  $B(p, p_\gamma)$ , this belief can be consistent with profitable deviation only if  $B(p, p_\gamma) = \gamma$ . It is thus reasonable to assume that, observing a deviating price  $p$ , consumers will hold belief  $B(p, p_\gamma) = \gamma$ . In other words, we require consumers' off-equilibrium belief to be consistent with firms' incentives:  $B(p, p_\gamma)$  is equal to the expected quality of firms that can (weakly) benefit from the deviation.<sup>13</sup>

Under passive belief, the consumer, who has arrived at a firm with price  $p$  and value  $u$ , will purchase from the firm if

$$\gamma u - p \geq \gamma u_\gamma - p_\gamma \geq 0.$$

Thus, the demand for the firm with price  $p$  from any visiting consumer, given that all other firms charge  $p_\gamma$ , is

$$D(p, p_\gamma) = 1 - F\left(\frac{\gamma u_\gamma + p - p_\gamma}{\gamma}\right),$$

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<sup>12</sup>Janssen and Ke (forthcoming) also assume a passive belief in a consumer search model in which firms may choose to provide a service that other firms can free-ride on. In their model, when observing a firm's deviation on service provision or/and price, consumers continue to believe that other firms maintain their equilibrium decisions

<sup>13</sup>In the literature on experience goods, firms can sometimes signal their quality through price and other devices (e.g., Choi, 1998; Riordan, 1988; Shapiro, 1983; Wernerfelt, 1988). In our model, given their qualities, firms are symmetric in all other aspects and there exist no signals that could potentially separate them. We will show formally in Proposition 1 below that there can be no "separating" equilibrium in our model for a given  $\gamma$ .

with  $D(p_\gamma, p_\gamma) = 1 - F(u_\gamma)$ . The profit for a firm of quality  $\beta$  from any visiting consumer,  $\pi(p, p_\gamma) = pD(p, p_\gamma)$ , is maximized when  $p$  satisfies

$$\frac{\partial \pi(p, p_\gamma)}{\partial p} = 1 - F\left(\frac{\gamma u_\gamma + p - p_\gamma}{\gamma}\right) - p \frac{1}{\gamma} f\left(\frac{\gamma u_\gamma + p - p_\gamma}{\gamma}\right) = 0.$$

At the uniform-price equilibrium,  $p = p_\gamma$ , and

$$p_\gamma = \gamma \frac{1 - F(u_\gamma)}{f(u_\gamma)}. \quad (5)$$

Moreover, if  $1 - F(u_\gamma)$  is log-concave, or, equivalently, the inverse hazard rate is (weakly) decreasing:

$$\lambda'(u) \leq 0 \quad \text{for } \lambda(u) \equiv \frac{1 - F(u)}{f(u)}, \quad (6)$$

then  $\pi(p, p_\gamma)$  is single-peaked at  $p_\gamma$ , the uniform-price equilibrium with  $p = p_\gamma$  exists uniquely, and  $p_\gamma$  is (weakly) lower when consumers search more intensively (i.e.,  $u_\gamma$  is higher). Moreover, at the unique  $p_\gamma$ ,

$$V_\gamma = \gamma u_\gamma - p_\gamma = \gamma u_\gamma - \gamma \lambda(u_\gamma) = \gamma [u_\gamma - \lambda(u_\gamma)].$$

The highest possible search cost ( $\bar{s}$ ) and its corresponding (lowest possible) reservation value ( $u_0$ ) are defined as

$$\bar{s} \equiv \gamma \int_{u_0}^{\bar{u}} (u - u_0) f(u) du, \quad \text{where} \quad u_0 \equiv \frac{1 - F(u_0)}{f(u_0)}. \quad (7)$$

Then, for any  $s < \bar{s}$ , there is a unique  $u_\gamma \in (0, \bar{u})$  that solves (4) and  $V_\gamma > 0$ , so that consumers will indeed engage in search when average firm quality in the market is  $\gamma \in [\beta_l, \beta_h]$ . We shall maintain assumptions (6) and  $s < \bar{s}$  throughout the paper.

In equilibrium, each firm's profit is

$$\pi_\gamma = \sum_i [F(u_\gamma)]^i p_\gamma D(p_\gamma, p_\gamma) = \gamma \lambda(u_\gamma),$$

where  $[F(u_\gamma)]^i$  is the number of consumers for whom the seller is their  $i$ 's visit. We measure consumer welfare and social welfare respectively by aggregate consumer surplus and total

surplus. For a market with a unit measure of consumers and of firms under average firm quality  $\gamma$ , industry profit, consumer welfare and social welfare are respectively:

$$\Pi_\gamma = \gamma\lambda(u_\gamma); \quad V_\gamma = \gamma[u_\gamma - \lambda(u_\gamma)]; \quad W_\gamma = \gamma u_\gamma. \quad (8)$$

The result below summarizes the above discussions and further establishes that there can be no equilibrium in which firms with different  $\beta$  charge different prices. At a potential “separating equilibrium” where  $\beta_h$  and  $\beta_l$  firms respectively charge  $p_h \neq p_l$ , following a deviating price  $p$  in the (small) neighborhoods of  $p_h$  or  $p_l$ , an assumption analogous to passive belief under the uniform-price equilibrium is that consumers believe the deviation to have been made by a  $\beta_h$  or  $\beta_l$  firm, respectively.

**Proposition 1** *There is a unique uniform-price equilibrium in the experience-goods market where average firm quality is  $\gamma$ . At the equilibrium, consumers search sequentially with reservation value  $u_\gamma$  and each firm charges price  $p_\gamma$ . Moreover, there can be no equilibrium where  $\beta_h$  and  $\beta_l$  firms respectively charge  $p_h \neq p_l$ , if consumers believe that a deviating price  $p$  in the neighborhoods of  $p_h$  or  $p_l$  is respectively made by a  $\beta_h$  or  $\beta_l$  firm.<sup>14</sup>*

A “separating” equilibrium with different prices for different  $\beta$  types cannot exist in our model, because there is nothing to enable such separation. Given average firm quality, the equilibrium in our search model of experience goods is essentially unique and is the uniform-price equilibrium.<sup>15</sup>

### 3.2 Impacts of Search Cost and Average Firm Quality

We next consider how the equilibrium may vary as search cost  $s$  or average firm quality  $\gamma$  changes. From (4), consumers’ reservation value,  $u_\gamma$ , increases in  $\gamma$  and decreases in  $s$ .

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<sup>14</sup>Our result that no separating equilibrium can exist also holds if, following a deviating price  $p$  at the proposed separating equilibrium, consumers believe that the deviating firm has quality  $\gamma$ , or, more generally, their off-equilibrium beliefs are respectively  $\alpha_h$  or  $\alpha_l$  for a deviating price  $p$  in the neighborhoods of  $p_h$  or  $p_l$ , with  $\alpha_h \geq \alpha_l$  and  $\beta_h/\alpha_h \geq \beta_l/\alpha_l$ .

<sup>15</sup>Search models are known to contain an equilibrium where all firms charge very high prices and no consumer engages in search. We do not consider such “uninteresting” equilibrium.

Because  $p_\gamma = \gamma \lambda(u_\gamma)$  and  $\lambda'(\cdot) \leq 0$ , it follows from (8) that, given  $\gamma$ ,  $p_\gamma$  and  $\Pi_\gamma$  increase in  $s$  whereas  $V_\gamma$  and  $W_\gamma$  decrease in  $s$ . Intuitively, a higher search cost reduces consumer search efficiency, which not only reduces consumers reservation value in search but also lessens competition and raises price. The higher price and lower search efficiency reduce consumer surplus, and the lower search efficiency also reduces social welfare; whereas higher price boosts profit.

From (8), clearly  $V_\gamma$  and  $W_\gamma$  increase in  $\gamma$ , the average quality of firms in the market. The effects of  $\gamma$  on price (and profit) are less obvious, as we can see, from (5):

$$\frac{dp_\gamma}{d\gamma} = \lambda(u_\gamma) + \gamma \lambda'(u_\gamma) \frac{\partial u_\gamma}{\partial \gamma},$$

where the first and the second terms on the RHS reflect, respectively, the positive (direct) demand effect and the negative (indirect) search effect on  $p_\gamma$  from an increase in  $\gamma$ . A higher  $\gamma$  lowers the price elasticity of demand for given  $u_\gamma$ <sup>16</sup>:

$$\eta = - \frac{\partial D(p, p_\gamma)}{\partial p} \frac{p}{D} \Big|_{p=p_\gamma} = \frac{p_\gamma}{\gamma \lambda(u_\gamma)},$$

which positively impact price; but it also increases the search reservation value  $u_\gamma$  and negatively impacts  $p_\gamma$  due to  $\lambda'(u_\gamma) \leq 0$ . Because

$$\frac{\partial u_\gamma}{\partial \gamma} = \frac{\int_{u_\gamma}^{\bar{u}} [1 - F(u)] du}{\gamma [1 - F(u_\gamma)]} < \frac{\bar{u} - u_\gamma}{\gamma},$$

a sufficient—but not necessary—condition for  $\frac{\partial p_\gamma}{\partial \gamma} > 0$  is

$$\frac{1}{\bar{u} - u_\gamma} \geq - \frac{\lambda'(u_\gamma)}{\lambda(u_\gamma)}, \quad (9)$$

which holds, for example, if  $F(u)$  is a uniform or exponential distribution. The proceeding discussions lead to the following:

**Corollary 1** *In equilibrium: (i) given average firm quality  $\gamma$ , price and profit increase, while consumer and social welfare decrease, in search cost  $s$ ; (ii) given  $s$ , a higher  $\gamma$  leads to higher price and profit if (9) holds, even though it intensifies search and price competition (i.e.,  $u_\gamma$  is higher and  $\lambda(u_\gamma)$  lower); moreover,  $V_\gamma$  and  $W_\gamma$  increase in  $\gamma$ .*

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<sup>16</sup>When  $\gamma$  is higher, the quality-adjusted price  $\frac{p}{\gamma}$  is lower and a marginal change in  $p$  is associated with less change in  $\frac{p}{\gamma}$  and hence leads to less change in the quantity demanded.

With exogenously-given firm quality for experience goods, the effects of search friction on price and welfare are similar to those in search markets for inspection goods.<sup>17</sup> Notably,  $p_\gamma$  increases in  $\gamma$  under (9), despite increased consumer search and price competition; this is in contrast to the result under search for inspection goods, to which we turn next.

### 3.3 Comparing with Search for Inspection Goods

To make comparison, we now consider inspection goods by assuming that, when searching a firm, a consumer will learn whether the firm's  $q$  is  $H$  or  $L$ , in addition to uncovering its price and  $u$ . Everything else is the same as in subsection 3.1. In particular,  $\beta \in \{\beta_l, \beta_h\}$  continues to be a firm's quality and remains to be its private information, with  $\gamma$  being the average firm quality in the market as defined in (1). We again look for a uniform-price equilibrium, where each firm charges price  $p_\gamma^I$ . As in subsection 3.1, consumers' optimal search follows a reservation-value strategy, with the optimal reservation value  $u_\gamma^I$  satisfying

$$\gamma \int_{u_\gamma^I}^{\bar{u}} (u - u_\gamma^I) f(u) du = s.$$

Interestingly, this condition is identical to condition (4) for experience goods. This is because when arriving at a firm with  $u = u_\gamma^I = u_\gamma$ , the expected marginal benefit of an additional search is the same under inspection and experience goods.<sup>18</sup> In other words, given  $\gamma$  and  $s$ ,  $u_\gamma = u_\gamma^I$ .

To determine the demand for each firm, suppose a firm deviates with price  $p$ . The passive belief assumption is now needed only for its part (ii)—other firms' price is still  $p_\gamma^I$ —because when searching the firm a consumer learns its product quality  $q$ . A visiting consumer will purchase from the firm if she finds  $q = H$  (which occurs with the firm's probability  $\beta$ ) and

$$u - p \geq u_\gamma^I - p_\gamma^I.$$

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<sup>17</sup>As we shall show in section 4, under endogenous firm quality and reputation, search costs have rather surprising welfare effects for experience goods, in contrast to those for inspection goods.

<sup>18</sup>However, as we shall see shortly, equilibrium consumer and social welfare are both higher for inspection than for experience goods, because for the former consumers can detect and hence avoid the utility loss from consuming a low quality product.



The firm's demand from any visiting consumer is thus

$$D^I(p, p_\gamma^I) = \beta [1 - F(u^I + p - p_1^I)],$$

and it chooses  $p$  to maximize  $pD^I(p, p_\gamma^I)$ , which, in equilibrium, leads to

$$p_\gamma^I = \frac{1 - F(u_\gamma^I)}{f(u_\gamma^I)} = \lambda(u_\gamma^I).$$

Since a random visit by a consumer to a firm will on average result in a purchase with probability  $\gamma [1 - F(u^I)]$ , and since all consumers—whose total mass is one—purchase, the equilibrium output of a firm with quality  $\beta$  is  $\frac{D^I(p^I, p_\gamma^I)}{\gamma [1 - F(u^I)]} = \frac{\beta}{\gamma}$ , and hence the firm's equilibrium profit is  $\pi^I(\beta) = \frac{\beta}{\gamma} \lambda(u_\gamma^I)$ . Thus, a firm will have a higher profit than an average firm if its quality  $\beta$  is higher than the market average, in contrast to the case of experience goods where a firm's equilibrium profit is independent of its  $\beta$ .

Notice that the price elasticity of demand here is independent of  $\gamma$ , in contrast to that for experience goods, which explains why  $p_\gamma^I$  does not depend on  $\gamma$  but  $p_\gamma$  does. Therefore, for inspection goods it is always true that

$$\frac{dp_\gamma^I}{d\gamma} = \lambda'(u_\gamma^I) \frac{\partial u_\gamma^I}{\partial \gamma} \leq 0,$$

in contrast to  $\frac{\partial p_\gamma}{\partial \gamma} > 0$  for experience goods under condition (9).

In equilibrium, industry profit, consumer surplus, and total welfare are respectively

$$\Pi_\gamma^I = \lambda(u_\gamma^I); \quad V_\gamma^I = u_\gamma^I - \lambda(u_\gamma^I); \quad W_\gamma^I = u^I. \quad (10)$$

Since  $u_\gamma^I = u_\gamma$ , comparing  $p_\gamma^I$  with  $p_\gamma$  and (10) with (8), we have:

**Proposition 2** *Given  $\gamma$  and  $s$ , consumers search with the same reservation value for inspection and experience goods, but  $V$ ,  $\Pi$ , and  $W$  are all lower for the latter. Higher  $\gamma$  leads to higher  $p$  for experience goods under condition (9) but to lower  $p$  for inspection goods. Moreover, a firm's profit increases in its  $\beta$  under inspection goods but is independent of its  $\beta$  under experience goods.*

For inspection goods, a higher average firm quality ( $\gamma$ ) in the market implies that consumers will have higher expected benefit from a search, because they are more likely to find an  $H$ -product. This boosts consumers' search incentive, as reflected by their higher search reservation value, which increases competition and leads to lower equilibrium price. Because consumers can observe product quality before purchase, an increase in  $\gamma$  will not affect a consumer's demand for a firm. By contrast, for experience goods, product quality is observed only after consumption, and thus higher  $\gamma$  also increases a consumer's expected utility from the product and hence the demand for it. Consequently, while a higher average firm quality similarly imposes a downward pressure on equilibrium price—by raising consumers' search reservation value—as for inspection goods, it has the additional demand effect that, on balance, results in higher equilibrium price under condition (9).

#### 4. ENDOGENOUS FIRM QUALITY AND REPUTATION

We now return to our full model with endogenous firm quality and reputation. Notice that if it is profitable for a firm with a higher  $x$  to make the quality investment, it must also be profitable for a firm with a lower  $x$  to do so. The equilibrium of our model will thus have the property that, for some threshold  $t$ , a firm will invest  $x$  to have  $\beta_h$  if  $x \leq t$  but will have  $\beta_l$  without the investment if  $x > t$ . We assume that  $\bar{x}$  is high enough so that in equilibrium  $t < \bar{x}$ ; i.e., some firms (with sufficiently high realizations of  $x$ ) will not incur  $x$ .

##### 4.1 Market Equilibrium

For a given  $t$ , the average firm quality ( $\beta$ ) in the market is

$$\gamma = \gamma(t) \equiv G(t) \beta_h + [1 - G(t)] \beta_l.$$

The first-period equilibrium is then the same as in our preliminary analysis of section 3 with  $\gamma = \gamma(t)$ , where consumers conduct sequential search with reservation value  $u_\gamma$  and all firms charge equilibrium price  $p_1^* = p_\gamma$ .

In the second period, consumers will observe product reviews from period-1 consumers.

For a firm of quality  $\beta$ , a portion  $\beta$  of its period-1 customers experienced quality  $H$  for its product. Thus, from the product reviews, period-2 consumers can correctly infer each firm's  $\beta$ .<sup>19</sup> There will thus effectively be two distinguishable segments of competing firms, one having quality  $\beta_h$  and another  $\beta_l$ . Comparing  $V_\gamma$  from (8) for  $\gamma = \beta_h$  and  $\gamma = \beta_l$ , consumers will clearly receive a higher surplus from—and thus only search—the segment of firms with  $\beta = \beta_h$ .<sup>20</sup> Thus, in equilibrium, consumers will all first search the segment of firms with  $\beta = \beta_h$ .

It follows that only  $\beta_h$  firms will be active sellers in the market in period 2, and consumers will search them with reservation value  $u_h \equiv u_h(s)$  that uniquely solves

$$\beta_h \int_{u_h}^{\bar{u}} (u - u_h) f(u) du = s. \quad (11)$$

Moreover, in equilibrium all  $\beta_h$  firms charge price

$$p_2^* = \beta_h \lambda(u_h), \quad (12)$$

and each earns profit

$$\pi_2^*(\beta_h) = \frac{\beta_h \lambda(u_h)}{G(t)},$$

where  $G(t)$  is the mass of  $\beta_h$  firms in the market. Firms with  $\beta_l$  earn zero profit in period 2.

We next consider the investment choices of firms and determine the threshold  $t$  on investment cost  $x$ . Given that firms invest  $x$  if and only  $x \leq t$ , if a firm with  $x$  acquires  $\beta_h$  at the beginning of period 1, it will earn discounted sum of profit

$$\pi_h = \gamma \lambda(u_\gamma) + \delta \frac{\beta_h \lambda(u_h)}{G(t)} - x. \quad (13)$$

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<sup>19</sup>We could allow product reviews to be noisy signals or consumer observations of product reviews in period 2 to be noisy signals as well. Our results will remain valid if the noisy signals are sufficiently accurate.

<sup>20</sup>This assumes that the equilibrium price in each segment is determined by equation (5) of Section 3. If all consumers believed the  $\beta_h$ -firms' price to be  $\infty$ , there could also be an equilibrium where they would only search  $\beta_l$  firms. We do not consider such possibility, same as we dismiss the trivial equilibrium where all consumer always choose not to participate in the market by believing that firms charge very high prices.

By contrast, if the firm chooses to maintain  $\beta_l$  without the investment, its expected profit is

$$\pi_l = \gamma \lambda(u_\gamma). \quad (14)$$

The equilibrium  $t = t^* \equiv t^*(s)$  is determined by the  $x$  at which  $\pi_h = \pi_l$ , or

$$\delta \beta_h \lambda(u_h) = t^* G(t^*). \quad (15)$$

Because average firm quality

$$\gamma \equiv \gamma(t^*) = \beta_h G(t^*) + \beta_l [1 - G(t^*)] \quad (16)$$

is endogenous, we modify the definition of  $\bar{s}$  in (7) by re-defining

$$\int_{u_0}^{\bar{u}} (u - u_0) f(u) du = \frac{\bar{s}}{\gamma(t^*(\bar{s}))}, \quad (17)$$

where  $u_0 \equiv \lambda(u_0) = \frac{1-F(u_0)}{f(u_0)}$ , to ensure consumer participation whenever  $s < \bar{s}$ .<sup>21</sup> Following the discussions above, we establish the result below by further showing the existence of  $t^*$  that solves equation (15).<sup>22</sup>

**Proposition 3** *Given  $s < \bar{s}$ , our model has an equilibrium where a firm has  $\beta = \beta_h$  if and only if its  $x \leq t^* = t^*(s)$ , and the average firm quality in period 1 is  $\gamma(t^*)$ . Consumers search with reservation value  $u_\gamma$  and pay price  $p_1^*$  in period 1, but search only  $\beta_h$  firms with reservation value  $u_h$  and pay  $p_2^*$  in period 2.*

The second-period industry profit, consumer surplus, and social welfare are respectively

$$\Pi_2^* = \beta_h \lambda(u_h); \quad V_2^* = \beta_h \phi(u_h); \quad W_2^* = \gamma u_h,$$

where we define  $\phi(u) \equiv [u - \lambda(u)]$ , with  $\phi(u) > 0$  and  $\phi'(u) \geq 1$ . Their corresponding discounted sums for the two periods are given by:

$$\Pi^* = \gamma \lambda(u_\gamma) + \delta \beta_h \lambda(u_h) - \int_0^{t^*} x dG(x); \quad (18)$$

$$V^* = \gamma \phi(u_\gamma) + \delta \beta_h \phi(u_h); \quad (19)$$

$$W^* = \gamma u_\gamma + \delta \beta_h u_h - \int_0^{t^*} x dG(x). \quad (20)$$

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<sup>21</sup> As we shall discuss shortly,  $\frac{\bar{s}}{\gamma(t^*(\bar{s}))}$  is likely to be monotonically increasing in  $s$ . If it is not, there might be multiple  $s$  that satisfies (17), in which case we define  $\bar{s}$  to be the smallest  $s$  among them.

<sup>22</sup> If  $\lambda(u)$  is strictly decreasing, then  $t^*$  is unique.

In equilibrium, each consumer receives positive (expected) surplus from market participation, and all firms receive positive profits, while the more efficient firms (with lower  $x$ , for  $x < t^*$ ) receive higher profits.

## 4.2 Welfare Effects of Search Cost

We now consider the welfare effects of search cost. Utilizing  $\frac{\partial u_h}{\partial s} = -\frac{1}{\beta_h[1-F(u_h)]}$  from (11),

$$\frac{\partial p_2^*}{\partial s} = \beta_h \lambda'(u_h) \frac{\partial u_h}{\partial s} = -\frac{\lambda'(u_h)}{[1-F(u_h)]} \geq 0.$$

Thus, as expected, a higher search cost leads to a higher price in period 2. Since

$$\frac{\partial t^*}{\partial s} = \frac{\delta \beta_H \lambda'(u_h) \frac{\partial u_h}{\partial s}}{G(t) + tg(t)} = \frac{-\delta \lambda'(u_h)}{G(t) + tg(t)} \frac{1}{[1-F(u_h)]} \geq 0, \quad (21)$$

and  $\frac{\partial \gamma(t^*)}{\partial t^*} = G'(t^*) (\beta_h - \beta_l) > 0$ , we have

$$\frac{\partial \gamma(t^*)}{\partial s} = \frac{\partial \gamma(t^*)}{\partial t^*} \frac{\partial t^*}{\partial s} \geq 0.$$

Thus, increases in search cost raise average firm quality.<sup>23</sup> Intuitively, when  $s$  is higher, price is higher, and a firm has higher profit in period 2 for being a  $\beta_h$  firm. That is, the return to the reputation of being a high quality firm is higher. This motivates more firms to invest in  $\beta_h$ , so that  $t^*$  becomes higher, which boosts  $\gamma$  in period 1.

When  $\gamma$  is given exogenously, a higher  $s$  leads to a lower  $u_\gamma$ , which in turn results in higher price and profit. With endogenous  $\gamma$ , changes in  $s$  also affect  $\gamma = \gamma(t^*)$ . While a higher  $s$  directly impacts  $u_\gamma$  negatively, it indirectly impacts  $u_\gamma$  positively through a higher  $\gamma$ . We expect that the direct effect of  $s$  would outweigh its indirect effect through  $\gamma$ , so that  $\frac{s}{\gamma}$  is higher with a higher  $s$ . Define the elasticity of average seller quality,  $\gamma$ , with respect to search cost as  $\varepsilon = \frac{s}{\gamma} \frac{\partial \gamma}{\partial s} = \frac{s}{\gamma} \frac{\partial \gamma}{\partial t^*} \frac{\partial t^*}{\partial s} \geq 0$ . Then

$$\frac{d\left(\frac{s}{\gamma}\right)}{ds} = \frac{\gamma - s \frac{\partial \gamma}{\partial s}}{\gamma^2} \geq 0 \iff \varepsilon \equiv \frac{\partial \gamma}{\partial s} \frac{s}{\gamma} \leq 1.$$

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<sup>23</sup>Notice that if  $\lambda'(u) = 0$ , then  $\partial t^*/\partial s = 0$ , and hence  $\partial \gamma(t^*)/\partial s = 0$ . Thus  $\lambda'(u) < 0$  is needed in order for average firm quality to (strictly) increase with  $s$ .

Thus, if  $\varepsilon \leq 1$ , then

$$\begin{aligned}\frac{\partial u_\gamma}{\partial s} &= \frac{\partial u_\gamma}{\partial (s/\gamma)} \frac{\partial (s/\gamma)}{\partial s} = \frac{\varepsilon - 1}{\gamma [1 - F(u_\gamma)]} \leq 0, \\ \frac{\partial p_\gamma}{\partial s} &= \gamma \lambda'(u_\gamma) \frac{\partial u_\gamma}{\partial s} \geq 0,\end{aligned}\tag{22}$$

and, since  $\delta \beta_h \lambda'(u_h) \frac{\partial u_h}{\partial s} = [t^* g(t^*) + G(t^*)] \frac{\partial t^*}{\partial s}$  from totally differentiating the two sides of (15), we have

$$\frac{\partial \Pi^*}{\partial s} = \frac{\partial p_\gamma}{\partial s} + \delta \beta_h \lambda'(u_h) \frac{\partial u_h}{\partial s} - t^* g(t^*) \frac{\partial t^*}{\partial s} = \frac{\partial p_\gamma}{\partial s} + G(t^*) \frac{\partial t^*}{\partial s} \geq 0.$$

The discussions above lead to:

**Remark 1**  $\gamma(t^*)$  and  $p_2^*$  increase in  $s$ , and so do  $p_1^*$  and  $\Pi^*$ , provided  $\lambda'(u) < 0$  and  $\varepsilon \leq 1$ .

Thus, with endogenous firm quality and reputation, search cost continues to be a key indicator of competition intensity, with increases in  $s$  leading to less competition and high prices in both periods. However, as we show next, search cost now has unconventional effects on consumer surplus and welfare. The result below refers to assumption

$$-M < \lambda'(u) < 0 \text{ for some } M > 0 \text{ and for } u \in [0, \bar{u}], \tag{23}$$

which strengthens condition (6). Condition (23) is satisfied, for instance, if  $F(u)$  is a uniform distribution, but it rules out the boundary case of the exponential distribution.

**Proposition 4** (i) Under condition (23), both  $V^*$  and  $W^*$  increase in  $s$  when  $s$  is sufficiently small. (ii) Suppose  $\varepsilon \leq 1$ . Then, when  $s \rightarrow \bar{s}$ ,  $V^*$  decreases in  $s$ , and so does  $W^*$  if  $u_0(\beta_h - \beta_l) \leq \bar{t}$ .

Therefore, higher search frictions can improve market performance for experience goods. To understand this striking result, notice that the effect of a marginal increase in  $s$  on consumer surplus can be decomposed as follows under conditions (23) and  $\varepsilon \leq 1$ :

$$\begin{aligned}\frac{\partial V^*}{\partial s} &= \underbrace{\frac{\partial \gamma}{\partial s} \phi(u_\gamma)}_{\text{average firm quality effect} > 0} + \underbrace{\gamma \phi'(u_\gamma) \frac{\partial u_\gamma}{\partial s}}_{\text{search efficiency effect in period 1} \leq 0} + \underbrace{\delta \beta_h \phi'(u_h) \frac{\partial u_h}{\partial s}}_{\text{search efficiency effect in period 2} < 0}.\end{aligned}$$

An increase in  $s$  raises the profit from being a  $\beta_h$  firm, motivating more firms to invest in quality and hence  $\gamma$  is higher in period 1. A higher  $s$  thus increases average firm quality in period 1. On the other hand, a higher  $s$  reduces  $u_h$  and, when  $\varepsilon \leq 1$ , also reduces  $u_\gamma$ ; that is, a higher search cost reduces search efficiency in both periods, which negatively impacts consumer surplus.

When search cost is low, price is low. Thus consumer surplus from an  $H$  product,  $\phi(u_\gamma)$ , is high, and the number of high quality firms (that incur  $x$ ) is small. In such situations, although a marginal increase in  $s$  raises prices only marginally, the profit increase from becoming a high quality firm is large because a  $\beta_h$  firm will have high sales in period 2. Hence, a marginal increase in  $s$  leads to a large increase in the number of high quality firms and in  $\gamma$  (i.e.,  $\frac{\partial \gamma}{\partial s}$  is high), which means that  $\frac{\partial \gamma}{\partial s} \phi(u_\gamma)$  is high, whereas the effect on search efficiency is more moderate. Thus the average firm quality effect dominates when  $s$  is small. On the other hand, when  $s$  is large, price is high. Thus  $\frac{\partial \gamma}{\partial s}$  and  $\phi(u_\gamma)$  are relatively low, so that the negative search efficiency effect dominates.

We can similarly decompose the effect of search cost on welfare as follows:

$$\frac{\partial W^*}{\partial s} = \underbrace{\frac{\partial \gamma}{\partial s} u_\gamma}_{\text{average firm quality effect} > 0} + \underbrace{\gamma \frac{\partial u_\gamma}{\partial s} + \delta \beta_h \frac{\partial u_h}{\partial s}}_{\text{search efficiency effect} < 0} + \underbrace{-t^* g(t^*) \frac{\partial t^*}{\partial s}}_{\text{investment cost effect} < 0}.$$

In addition to the average firm quality and search efficiency effects, as in the case of consumer surplus, for  $W^*$  there is the additional effect of investment cost: a higher search cost increases the total investment cost for  $\beta_h$ , because the higher profit from being a high-quality firm from an increase in  $s$  leads to more firms to invest in  $\beta_h$ . But when  $s \rightarrow 0$ ,  $t^* \rightarrow 0$ , and thus the additional effect of investment cost vanishes so that  $W^*$  increases in  $s$ , similarly as for  $V^*$ . On the other hand, when  $s \rightarrow \bar{s}$ , the highest possible value of search cost,  $t^* \rightarrow \bar{t}$  and  $u_\gamma \rightarrow u_0$ . If  $u_0(\beta_h - \beta_l) < \bar{t}$ , then the investment cost effect (alone) dominates the average firm quality effect, and hence  $W^*$  decreases in  $s$ , similarly as for  $V^*$ .<sup>24</sup>

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<sup>24</sup>The conclusions in Proposition 4 can be strengthened if we impose additional assumptions. We have

Our finding that both consumer and total welfare are initially increasing in search cost is in sharp contrast to the result in the existing search literature, where consumer and social welfare monotonically decrease as search cost increases. Both endogenous firm quality and the experience nature of goods are important for the non-monotonic result in our model. If average firm quality in the market ( $\gamma$ ) is exogenously given, higher search costs would only have the negative effect of reducing search efficiency. In our model, an increase in search cost has the additional effect of inducing a higher  $\gamma$ , which positively impacts consumer and social welfare, and it is the dominant force when search cost is low. However, if the goods were inspection goods, even with endogenous product quality, both consumer and social welfare would decrease with search cost, as we show next.

### 4.3 Comparing to Welfare for Inspection Goods

For inspection goods, same as in the case of experience goods, for a given  $t$  the average firm quality in the market is

$$\gamma = \gamma(t) = G(t) \beta_h + [1 - G(t)] \beta_l.$$

The first-period equilibrium is then the same as in subsection 3.3, with consumers conducting sequential search under reservation value  $u_\gamma^I = u_\gamma$  and all firms charging  $p_1^I = p_\gamma^I$ . Notice that a firm of quality  $\beta$  earns profit  $\frac{\beta}{\gamma} \lambda(u_\gamma^I)$  in period 1.

Suppose also that, as for experience goods, in period 2 consumers can observe first-period consumers' product reviews, which reveal each firm's  $\beta$ .<sup>25</sup> Then, in period 2, consumers will also only search  $\beta_h$  firms, with reservation value  $u_h$ . Moreover, from subsection 3.3,  $\beta_h$  sellers will charge  $p_2^I = \lambda(u_h)$ , each earning profit  $\frac{1}{G(t)} \lambda(u_h)$  in period 2 if the number of  $\beta_h$  firms is  $G(t)$ . Thus, a  $\beta_h$  seller earns higher profits in both periods.

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verified, for example, that both  $V^*$  and  $W^*$  exhibit an inverted-U shape as  $s$  increases when  $F(u)$  and  $G(x)$  are uniform distributions under plausible parameter values.

<sup>25</sup>Since consumers observe  $q \in \{H, L\}$  when searching a firm, they will only purchase if  $q = H$ . A consumer's review in this case is still about whether a firm's product quality  $q$  is  $H$  or  $L$ ; even though she does not purchase if the product quality turns out to be low, the consumer has wasted a costly search if  $q = L$ .



In equilibrium, a firm will invest in  $\beta_h$  if and only if  $x \leq \tau$ , where the cutoff value  $\tau$  is determined by

$$\frac{\beta_h}{\gamma} \lambda(u_\gamma^I) + \delta \frac{1}{G(\tau)} \lambda(u_h) - \tau = \frac{\beta_l}{\gamma} \lambda(u_\gamma^I),$$

or

$$\tau = \frac{\beta_h - \beta_l}{\gamma(\tau)} \lambda(u_\gamma) + \delta \frac{1}{G(\tau)} \lambda(u_h). \quad (24)$$

Thus, same as for experience goods, a higher  $s$ , which increases  $\lambda(u_\gamma)$  and  $\lambda(u_h)$ , will raise average firm quality  $\gamma(\tau)$ . Industry profit, consumer surplus, and social welfare for the two periods together are respectively

$$\Pi^I = \lambda(u_\gamma) + \delta \lambda(u_h) - \int_0^\tau x dG(x); \quad V^I = \phi(u_\gamma) + \delta \phi(u_h); \quad W^I = u_\gamma + \delta u_h - \int_0^\tau x dG(x),$$

where we recall  $\phi(u) = u - \lambda(u)$ .

The effect of search cost on consumer welfare under inspection goods is always negative (provided  $\varepsilon \leq 1$  so that  $d\left(\frac{s}{\gamma}\right)/ds \geq 0$ ), because the positive average firm quality effect for experience goods is absent:

$$\frac{\partial V^I}{\partial s} = \underbrace{\phi'(u_\gamma) \frac{\partial u_\gamma}{\partial s}}_{\text{search efficiency effect in period 1} \leq 0} + \underbrace{\delta \phi'(u_h) \frac{\partial u_h}{\partial s}}_{\text{search efficiency effect in period 2} < 0} < 0.$$

Similarly,

$$\frac{\partial W^I}{\partial s} = \underbrace{\gamma \frac{\partial u_\gamma}{\partial s} + \delta \beta_h \frac{\partial u_h}{\partial s}}_{\text{search efficiency effect} < 0} + \underbrace{-\tau g(\tau) \frac{\partial \tau}{\partial s}}_{\text{investment cost effect} < 0} < 0.$$

We thus have:

**Remark 2** *For inspection goods, consumer and total welfare monotonically decrease in search cost, in contrast to the result for experience goods.*

For both inspection and experience goods, an increase in search cost leads to higher price and hence to higher return for quality reputation because only  $\beta_h$  firms sell in period 2. However, consumers can avoid the loss from a low-quality product for inspection goods but not for experience goods. Thus, the marginal benefit from increasing firm quality ( $\gamma$ ) due to

a higher  $s$ , for consumers and for social welfare, is lower for inspection than for experience goods. This explains why a higher  $s$  can lead to higher consumer and social welfare through the positive quality effect for experience but not for inspection goods.

#### 4.4 Equilibrium vs. Efficient Quality Investment

We further investigate how the equilibrium quality investment compares with the social optimum, by comparing the cutoff values for quality investment ( $t$ ) in these two cases. The result below shows that the equilibrium cutoff ( $t^*$ ) can be higher or lower than the efficient value ( $t^o$ ) when search cost is sufficiently high or low, respectively.

**Proposition 5** *Given  $s \in (0, \bar{s})$ , there exists  $t^o > 0$  that maximizes total welfare. Moreover, provided  $t^o < \bar{t}$ , there exists a unique  $\sigma > 0$  such that  $t^* \leq t^o$  if  $s \leq \sigma$  but  $t^* > t^o$  if  $\sigma < s \leq \bar{s}$ .*

An increase in  $t$  results in a higher proportion of firms that invest. This leads to a higher expected quality of sellers and hence higher welfare in the first period, as reflected by a higher  $\gamma u_\gamma$ . On the other hand, investment is costly, and a higher  $t$  leads to higher investment cost  $\int_0^t x dG(x)$ . A socially optimal  $t^o$  balances these two opposing forces, with the marginal benefit from a higher  $\gamma$  being equal to the marginal cost of increasing  $t$ . From the definition of  $\bar{t}$  in (36), we note that  $\bar{t} > 0$  is independent of  $\beta_l$  whereas  $t^o \rightarrow 0$  if  $\beta_l \rightarrow \beta_h$ . Thus  $t^o < \bar{t}$  when  $(\beta_h - \beta_l)$  is relatively small so that the benefit from high quality ( $\beta_h$ ) is more limited.

When a firm chooses to invest in quality (to incur  $x$ ), it internalizes neither the positive impact on consumers from a higher  $\gamma$  nor the negative impact on other firms' profits. When  $s$  is low, consumers have strong search incentives and  $u_\gamma - p_\gamma$  is high, so that a higher average firm quality  $\gamma$  (i.e. a higher  $t$ ) has a large impact on  $\gamma(u_\gamma - p_\gamma)$  and the positive consumer externality dominates. Therefore  $t^* < t^o$  when  $s$  is low. On the other hand, when  $s$  is high,  $u_\gamma - p_\gamma$  is low and welfare gain from increasing  $\gamma$  is relatively small (so  $t^o$  is relatively low), whereas price is high and the negative "profit shifting" effect tends to dominate, so that  $t^*$  tends to exceed  $t^o$ .

In the existing literature on experience goods (with no search cost), product quality is usually inefficiently low because the market often creates other distortions (such as inefficiently high price) in order to induce firms to improve quality. This is consistent with our result that equilibrium product quality is deficient ( $t^* \leq t^o$ ) when search cost  $s$  is sufficiently small. However, our result also shows that there can be socially excessive quality investment in the presence of (substantial) search frictions.

It can be verified that a result similar to Proposition 5 also holds for inspection goods. Thus, quality provision is socially deficient when  $s$  is low but possibly excessive when  $s$  is high, for both experience and inspection goods in search markets. One notable difference is that the profit-shifting effect of a firm's quality investment arises only in period 2 for experience goods, whereas it also arises in period 1 for inspection goods, because consumers' purchases in period 1 are affected by product quality only for the latter. This suggests that equilibrium product quality is more likely to be deficient for experience than for inspection goods.

## 5. IMPACT OF AN INTERMEDIARY

In many markets, consumers search their products through an intermediary that serves as a search platform, such as Amazon.com and booking.com. We now extend our model to include such an intermediary.<sup>26</sup> A profit-maximizing intermediary can affect market outcomes by charging sellers fees for being on its platform, which may in turn affect the (average) quality of sellers on the marketplace, search efficiency, and market price.<sup>27</sup> We show that the intermediary can improve welfare by screening out low-quality sellers, especially when

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<sup>26</sup>Athey and Ellison (2011) and Chen and He (2011) study position auctions by search engines, emphasizing their beneficial role as information intermediary. Bagwell and Ramey (1996) pioneered the study of coordination economies in retail market search. Others have shown that search intermediaries need not (optimally) improve search efficiency (e.g. Eliaz and Spiegler, 2011; White, 2013; de Cornière and Taylor, 2014). None of the above analyze experience goods.

<sup>27</sup>In addition to providing a search platform, the intermediary may publish product reviews by customers. The intermediary can thus be a reputation carrier, enabling firms to establish quality reputation when product reviews are otherwise unavailable.

it can commit to a relatively small listing space on the platform, but the intermediary may lower welfare when it lacks such commitment ability.

Suppose that the intermediary can charge each seller  $(k, \mu)$ , where  $k \geq 0$  is a fixed fee and  $\mu \geq 0$  is a percentage of the transaction price. Sellers that pay the fees will have access to consumers associated with the intermediary. We further assume that there is a minimum platform size  $\Omega \in (0, 1]$ —number of sellers to be listed on the platform—that the intermediary can commit to.<sup>28</sup>

The timing of the extended model is as follows. The intermediary first chooses  $(k, \mu)$ . In period 1, after its realization of  $x$ , each seller chooses whether to pay the fees to sell on the platform and decides whether to invest  $x$  to become a seller with  $\beta_h$ . Sellers on the platform then set prices, consumers sequentially search sellers on the platform, and transactions are made. In period 2, consumer reviews from previous period are available to the current cohort of consumers. Sellers on the platform set prices, and consumers again sequentially search sellers on the platform and possibly make purchases. Everything else about the model is the same as in section 2.<sup>29</sup> Notice that sellers not on the platform are not active in either period.

Given the average firm quality on the platform,  $\gamma$ , which is endogenously determined by the firms on the platform who will invest in  $\beta_h$ , the firms' pricing and consumers' search strategies are the same as in section 4, unaffected by the values of  $k$  and  $\mu$ . In particular, at a uniform-price equilibrium, the optimal consumer search rule is again given by (17), whereas a seller will choose  $p$  to maximize  $(1 - \mu)pD(p, p^*)$ , the solution of which does not depend on  $\mu$ .

There are two possible types of equilibria for a given  $\Omega$ , depending on its value: (1) a separating equilibrium in which all sellers on the platform are of high quality ( $\beta_h$ ), and (2) a pooling equilibrium in which both high and low quality sellers are present on the platform.

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<sup>28</sup>A similar assumption is adopted by, for example, Eliaz and Spiegler (2011) under a continuum of sellers, or Athey and Ellison (2011) and Chen and He (2011) under a finite number of sellers.

<sup>29</sup>For convenience, we assume that each search still costs  $s$ . The analysis can be easily extended to situations where  $s$  becomes lower when consumers search on the platform.

First, at a separating equilibrium, the intermediary charges high fees such that only high quality sellers will be able to earn positive profit. Suppose that in equilibrium, there is a cutoff value  $t_k$  such that only sellers with  $x \leq t_k$  choose to invest in  $\beta_h$  and pay to be listed on the platform while other sellers are off the platform and inactive. In this case, in equilibrium the intermediary solves the following problem (P1):

$$\max_{(k, \mu)} \Psi = kG(t_k) + \mu\beta_h\lambda(u_h)(1 + \delta),$$

subject to

$$(1 - \mu) \frac{1}{G(t_k)} \beta_h \lambda(u_h) - k < 0, \quad (25)$$

$$(1 - \mu) \frac{1}{G(t_k)} \beta_h \lambda(u_h) (1 + \delta) - k - x \geq 0 \quad \text{for } x \leq t_k, \quad (26)$$

where the first constraint ensures that a seller with  $\beta_l$  has no incentive to be on the platform (being able to sell only in period 1) and the second constraint ensures that sellers with low  $x$  find it profitable to acquire  $\beta_h$  and sell on the platform for two periods.

Define  $t_\Omega$  and  $\hat{t}$  respectively as

$$G(t_\Omega) = \Omega; \quad \hat{t} = \frac{1}{G(\hat{t})} \beta_h \lambda(u_h) (1 + \delta), \quad (27)$$

and, for  $\bar{t}$  defined in (36), we assume  $\max\{t_\Omega, \hat{t}\} < \bar{t} < \bar{x}$ . Then, exactly  $\Omega$  firms will be listed on the platform if and only if all firms with  $x \leq t_\Omega$  pay  $(k, \mu)$  and invest  $x$ , whereas  $G(\hat{t})$  is the mass of firms who will acquire  $\beta_h$  and be on the platform if  $k = \mu = 0$  and  $\gamma = \beta_h$ .

**Lemma 1** *Suppose  $t_\Omega \leq \hat{t}$ . There is a separating equilibrium in which the intermediary optimally sets  $\mu^* = 0$  and*

$$k^* = \frac{1}{G(t_\Omega)} \beta_h \lambda(u_h) (1 + \delta) - t_\Omega; \quad (28)$$

*whereas only firms with  $x \leq t_\Omega$  choose to acquire  $\beta_h$  and sell on the platform. Moreover, the presence of the intermediary improves welfare if  $t_\Omega \leq t^*$ , with  $t^*$  defined in (15) and  $t^* < \hat{t}$ .*

Given (relatively small)  $\Omega$  so that  $\hat{t} \geq t_\Omega$ , the intermediary can screen out low quality firms by charging high fees and thus organize a platform that contains only high quality sellers. At this equilibrium, search efficiency is higher in period 1 (and is unchanged in period 2) as compared to the market equilibrium without the intermediary; if additionally  $t_\Omega \leq t^*$ , then the total investment cost on quality is also (weakly) lower—and hence social welfare must be higher—at the separating equilibrium.

We next consider an alternative possible equilibrium, a pooling equilibrium, which arises when  $t_\Omega > \hat{t}$ . In this equilibrium, there is a cutoff value  $t_k$  such that only firms with  $x \leq t_k$  choose to acquire  $\beta_h$ , but all firms will pay to be on the platform. The intermediary solves the following maximization problem (P2):

$$\max_{k, \mu} \Psi = k + \mu [\gamma(t_k) \lambda(u_\gamma) + \delta \beta_h \lambda(u_h)],$$

subject to

$$(1 - \mu) \gamma(t_k) \lambda(u_\gamma) - k \geq 0, \quad (29)$$

$$(1 - \mu) \delta \frac{1}{G(t_k)} \beta_h \lambda(u_h) - x \geq 0 \quad \text{for } x \leq t_k, \quad (30)$$

where the two constraints ensure respectively that firms with  $\beta_l$  are willing to pay  $(k, \mu)$  and that firms with  $x \leq t_k$  will additionally choose to acquire  $\beta_h$ . The result below refers to condition

$$\left( \lambda(u_\gamma) - \lambda'(u_\gamma) \frac{s}{\gamma} \frac{1}{1 - F(u_\gamma)} \right) (\beta_h - \beta_l) \leq t^* \quad (31)$$

for  $\gamma = \gamma(t^*)$ , which holds if  $(\beta_h - \beta_l)$  is not too large.

**Lemma 2** *Suppose  $t_\Omega > \hat{t}$  and (31) holds. Then, there exists a pooling equilibrium with  $t_k^* \in (0, t^*)$ . The intermediary optimally chooses*

$$k^* = (1 - \mu^*) \gamma(t_k^*) \lambda(u_\gamma); \quad \mu^* = 1 - t_k^* G(t_k^*) \frac{1}{\delta \beta_h} \lambda(u_h);$$

*and all firms choose to be on the platform. However, only firms with  $x \leq t_k^*$  choose to acquire  $\beta_h$ .*

When the minimum platform size  $\Omega$  is relatively large and  $(\beta_h - \beta_l)$  relatively small, there is a pooling equilibrium in which the intermediary finds optimal to accommodate both high and low quality firms, with positive  $k$  and  $\mu$ . Due to  $\mu^* > 0$ , however,  $t_k^* < t^*$  and the average firm quality in period 1 is lower than when the intermediary is absent. The intermediary can thus lower welfare if it leads to a pooling equilibrium, because the market provision of quality may be already too low without the intermediary.

Combining Lemma 1 and Lemma 2, noting  $t^* < \hat{t}$  and recalling from Proposition 5 that  $t^* < t^o$  if  $s < \sigma$ , we have

**Proposition 6** *For the extended model with an intermediary, assume  $\max\{t_\Omega, \hat{t}\} < \bar{t}$ . (i) If  $t_\Omega < \hat{t}$ , then it is an equilibrium for firms with  $x \leq t_\Omega$  to acquire  $\beta_h$  and be listed by the intermediary, with the intermediary improving social welfare. (ii) If  $t_\Omega > \hat{t}$ , then it is an equilibrium for all firms to be listed by the intermediary but only those with  $x \leq t_k^* < t^*$  to acquire  $\beta_h$ ; and if  $s < \sigma$ , then  $t_k^* < t^* < t^o$ , so that the market provision of quality is further below the social optimum.<sup>30</sup>*

The presence of a profit-maximizing search intermediary can thus either increase or decrease welfare.<sup>31</sup> Notice that  $t_\Omega < t^*$  is more likely to hold if  $s$  is relatively large, while  $t_\Omega > \hat{t}$  and  $s < \sigma$  are more likely to hold if  $s$  is relatively small. Therefore, the presence of the intermediary is more likely to increase welfare when the intermediary can commit to a relatively small minimum listing size or under relatively large search cost; but it can reduce welfare when the minimum listing space on the search platform is relatively large and search cost is relatively low.<sup>32</sup>

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<sup>30</sup>In this case, social welfare, same as  $W^*$  from (20), is likely—but not necessarily—lower under  $t_k^*$  than under  $t^*$ . If  $W^*$  is monotonically increasing in  $t$  for  $t < t^o$ , which for example is true when  $F(\cdot)$  and  $G(\cdot)$  are uniform distributions, then  $W^*$  is unambiguously lower under  $t_k^*$  than under  $t^*$  if  $t_k^* < t^* < t^o$ .

<sup>31</sup>As discussed in subsection 4.3, for inspection goods a firm's profit is higher when it has higher quality. Thus, under an intermediary it is likely that a separating equilibrium prevails, with only the high-quality firms being present on the search platform in both periods. The intermediary will then improve welfare, as in Chen and He (2011) and Athey and Ellison (2011). To be more focused, we have not analyzed this case.

<sup>32</sup>We have verified numerically that, for example, if  $F(u)$  and  $G(x)$  are both uniform distributions, then

## 6. CONCLUSION

This paper has studied a search model of experience goods. We find that search frictions impact price competition and market performance very differently for experience goods. Specifically, in contrast to the results for inspection goods, a higher average firm quality raises equilibrium price despite intensifying consumer search, and an increase in search cost can boost both consumer and social welfare. We also find that equilibrium quality investment is deficient when search cost is low but can be excessive when search cost is high. Moreover, a search intermediary can improve welfare by committing to a sufficiently limited space for displaying sellers, but it may reduce welfare if it is unable to do so.

Importantly, because consumers cannot observe product quality before purchase for experience goods, they benefit more when a firm's product is more likely of high quality. This provides the main intuition for why in our model (i) a higher expected firm quality raises market price (by making demand for each firm less elastic), even though the intensified consumer search would otherwise lower price (as it would for inspection goods), and (ii) a higher search cost, which decreases search efficiency but raises average firm quality, can increase welfare for experience but not for inspection goods. Search friction and product quality uncertainty are crucial features of many consumer markets. Our results shed new light on how search markets function under quality uncertainty.

## APPENDIX

The appendix contains proofs for Propositions 1, 3, 4, 5 and for Lemmas 1 and 2.

**Proof of Proposition 1.** It suffices to show that there can be no equilibrium where  $\beta_h$  and  $\beta_l$  firms charge different prices. Suppose, to the contrary, that there is an equilibrium where  $\beta_h$  and  $\beta_l$  firms charge  $p_h \neq p_l$ . Then the equilibrium profit for the two types of firms must be equal,  $\pi_h = \pi_l$ , because otherwise a firm of the type with a lower profit, say,  $\beta_l$ , can deviate to  $p_h$  and increase its profit. So suppose  $p_h \neq p_l$  but  $\pi_h = \pi_l$ . We show that there are plausible parameter values under which  $\max\{t_\Omega, \hat{t}\} < \bar{t}$  and the intermediary increases welfare when  $\Omega$  is small but decreases welfare when  $\Omega$  is relatively large.



this leads to a contradiction.

Let each consumer's reservation values be  $u_h$  and  $u_l$  at a  $\beta_h$  and a  $\beta_l$  firm, respectively. Then, since the consumer has the same continuation value at both types of firms, we have

$$\beta_h u_h - p_h = \beta_l u_l - p_l. \quad (32)$$

Moreover, reservation values  $u_h$  and  $u_l$  satisfy the following equation

$$G \int_{u_h}^{\bar{u}} \beta_h (u - u_h) f(u) du + (1 - G) \int_{u_l}^{\bar{u}} \beta_l (u - u_l) f(u) du = s, \quad (33)$$

in which the LHS is the expected gain from one more search: When the consumer is currently at a  $\beta_h$  firm (having  $u_h$  and  $p_h$ ), with probability  $G$  she will encounter another  $\beta_h$  firm with gain  $(\beta_h u - p_h) - (\beta_h u_h - p_h) = \beta_h (u - u_h)$ , conditional on her  $u > u_h$  from the new firm searched, while with probability  $(1 - G)$  the consumer will encounter a  $\beta_l$  firm with gain  $(\beta_l u - p_l) - (\beta_h u_h - p_h)$ , which equals  $\beta_l (u - u_l)$  from (32), conditional on  $u > u_l$ . The argument is similar when the consumer is currently at a  $\beta_l$  firm (having  $u_l$  and  $p_l$ ).

Next, given consumers' search behavior and the pricing strategies of other firms, if a  $\beta_h$  firm deviates with price  $p$  in the neighborhoods of  $p_h$ , under our assumption consumers will believe that the deviation is made by the  $\beta_h$  firm. Hence, at the deviating price  $p$ , a consumer with value  $u$  at the  $\beta_h$  firm will purchase if  $\beta_h u - p \geq (G) [\beta_h u_h - p_h] + (1 - G) [\beta_l u_l - p_l] = \beta_h u_h - p_h$ . The firm's demand from any visiting consumer is thus  $1 - F\left(u_h + \frac{p - p_h}{\beta_h}\right)$ . Solving  $\max_p p \left[1 - F\left(u_h + \frac{p - p_h}{\beta_h}\right)\right]$ , with  $p = p_h$  in equilibrium, we obtain  $p_h = \beta_h \lambda(u_h)$ . Similarly,  $p_l = \beta_l \lambda(u_l)$ . Therefore

$$\beta_h u_h - p_h = \beta_h [u_h - \lambda(u_h)]; \quad \beta_l u_l - p_l = \beta_l [u_l - \lambda(u_l)],$$

and from (32) we obtain

$$\beta_h [u_h - \lambda(u_h)] = \beta_l [u_l - \lambda(u_l)]. \quad (34)$$

Furthermore:

$$\pi_h = \frac{p_h [1 - F(u_h)]}{1 - (G) F(u_h) - (1 - G) F(u_l)}, \quad \pi_l = \frac{p_l [1 - F(u_l)]}{1 - (G) F(u_h) - (1 - G) F(u_l)}. \quad (35)$$

If  $p_h > p_l$ , then  $\pi_h = \pi_l$  implies  $u_h > u_l$ , which further implies  $\beta_h [u_h - \lambda(u_h)] > \beta_l [u_l - \lambda(u_l)]$  since  $\lambda'(\cdot) \leq 0$ . This contradicts (34). If  $p_h = \beta_h \lambda(u_h) < p_l = \beta_l \lambda(u_l)$ , then from  $\beta_h > \beta_l$  and  $\lambda'(\cdot) \leq 0$  we have  $u_h \geq u_l$  and hence

$$\beta_h u_h - \beta_h \lambda(u_h) > \beta_l u_l - \beta_l \lambda(u_l),$$

again contradicting (34). ■

**Proof of Proposition 3.** The RHS of equation (15) increases in  $t^*$ , whereas the LHS of equation (15) is larger than the RHS when  $t^* \rightarrow 0$ . Moreover, define  $\bar{t}$  as

$$\delta \beta_h \lambda(u_h(\bar{s})) = \bar{t} G(\bar{t}). \quad (36)$$

Since  $\lambda(u_h)$  weakly increases in  $s$ , we have  $\delta \beta_h \lambda(u_h(s)) \leq \bar{t} G(\bar{t})$  for all  $s \in (0, \bar{s})$ . Thus, the LHS of equation (15) is no higher than the RHS when  $t^* \rightarrow \bar{t}$ . Therefore, there exists  $t^* \in (t, \bar{t})$  that solves equation (15). ■

**Proof of Proposition 4.** (i) First, from (19),

$$\frac{\partial V^*}{\partial s} = \frac{\partial \gamma}{\partial s} \phi(u_\gamma) + \gamma \phi'(u_\gamma) \frac{\partial u_\gamma}{\partial s} + \delta \beta_h \phi'(u_h) \frac{\partial u_h}{\partial s}.$$

Since  $\frac{\partial u_\gamma}{\partial(s/\gamma)} = -\frac{1}{[1-F(u_\gamma)]}$  from (4) and from (21):

$$\frac{\partial \gamma}{\partial s} = \frac{\partial \gamma}{\partial t^*} \frac{\partial t^*}{\partial s} = (\beta_h - \beta_l) g(t^*) \frac{-\delta \lambda'(u_h)}{G(t^*) + t^* g(t^*)} \frac{1}{[1 - F(u_h)]}.$$

With  $\frac{\partial u_\gamma}{\partial s} = \frac{\varepsilon - 1}{\gamma [1 - F(u_\gamma)]}$  from (22) and  $\frac{\partial(s/\gamma)}{\partial s} = \frac{1 - \varepsilon}{\gamma}$ , we then have

$$\begin{aligned} \frac{\partial V^*}{\partial s} &= (\beta_h - \beta_l) g(t^*) \frac{-\delta \lambda'(u_h)}{G(t^*) + t^* g(t^*)} \frac{\phi(u_\gamma)}{[1 - F(u_h)]} + \frac{\phi'(u_\gamma)(\varepsilon - 1)}{[1 - F(u_\gamma)]} - \delta \frac{\phi'(u_h)}{[1 - F(u_h)]} \\ &\geq \frac{1}{[1 - F(u_h)]} \left[ (\beta_h - \beta_l) \frac{-\delta \lambda'(u_h) \phi(u_\gamma)}{\frac{G(t^*)}{g(t^*)} + t^*} - \phi'(u_\gamma) - \delta \phi'(u_h) \right], \end{aligned} \quad (37)$$

where the inequality holds because  $\varepsilon \geq 0$  and  $[1 - F(u_\gamma)] \geq [1 - F(u_h)]$ . When  $s \rightarrow 0$ :  $\frac{G(t^*)}{g(t^*)} \rightarrow 0$ ,  $u_h \rightarrow \bar{u}$ ,  $u_\gamma \rightarrow \bar{u}$ ;  $\lambda'(\bar{u}) < 0$ ,  $\phi(u_\gamma) \rightarrow \bar{u}$ ; and  $(\beta_h - \beta_l) \frac{-\delta \lambda'(u_h) \phi(u_\gamma)}{\frac{G(t^*)}{g(t^*)} + t^*} \rightarrow \infty$ . Thus, since  $\phi'(u) = 1 - \lambda'(u)$  is bounded for any  $u$ , we have  $\frac{\partial V^*}{\partial s} > 0$  as  $s \rightarrow 0$ .

Next, from (20),

$$\begin{aligned}
\frac{\partial W^*}{\partial s} &= \frac{\partial \gamma}{\partial s} u_\gamma + \gamma \frac{\partial u_\gamma}{\partial s} + \delta \beta_h \frac{\partial u_h}{\partial s} - t^* g(t^*) \frac{\partial t^*}{\partial s} \\
&= [u_\gamma (\beta_h - \beta_l) - t] g(t) \frac{\partial t}{\partial s} + (\varepsilon - 1) \frac{1}{1 - F(u_\gamma)} - \delta \frac{1}{1 - F(u_h)} \\
&= [u_\gamma (\beta_h - \beta_l) - t^*] \frac{-\delta \lambda'(u_h)}{t^* + \frac{G(t^*)}{g(t^*)}} \frac{1}{1 - F(u_h)} + (\varepsilon - 1) \frac{1}{1 - F(u_\gamma)} - \delta \frac{1}{1 - F(u_h)} \\
&> \frac{1}{1 - F(u_h)} \left\{ [u_\gamma (\beta_h - \beta_l) - t^*] \frac{-\delta \lambda'(u_h)}{t^* + \frac{G(t^*)}{g(t^*)}} - 1 - \delta \right\},
\end{aligned}$$

where the last inequality is due to  $\varepsilon \geq 0$  and  $u_\gamma \leq u_h$ . When  $s \rightarrow 0$ ,  $t^* \rightarrow 0$ ,  $\frac{G(t^*)}{g(t^*)} \rightarrow 0$ ,  $u_\gamma \rightarrow \bar{u}$ , and hence  $[u_\gamma (\beta_h - \beta_l) - t^*] \frac{-\delta \lambda'(u_h)}{t^* + \frac{G(t^*)}{g(t^*)}} \rightarrow \infty$ . Thus  $\frac{\partial W^*}{\partial s} > 0$  as  $s \rightarrow 0$ .

(ii) First,  $\frac{\partial u_h}{\partial s} < 0$ ,  $\lambda'(u) \leq 0$ ,  $\frac{\partial u_\gamma}{\partial s} \leq 0$  if  $\varepsilon \leq 1$ ; and, when  $s \rightarrow \bar{s}$ ,  $\phi(u_\gamma) = [u_\gamma - \lambda(u_\gamma)] \rightarrow 0$ . Hence, from (37), if  $\varepsilon \leq 1$ ,  $\frac{\partial W^*}{\partial s} < 0$  as  $s \rightarrow \bar{s}$ .

Next, when  $s \rightarrow \bar{s}$ ,  $u_\gamma \rightarrow u_0$ ,  $t^* \rightarrow \bar{t}$ , and hence  $\frac{\partial W^*}{\partial s} < 0$  if  $\bar{t} \geq u_0 (\beta_h - \beta_l)$  and  $\varepsilon \leq 1$ . ■

**Proof of Proposition 5.** Recall  $\frac{\partial \gamma}{\partial t} = (\beta_h - \beta_l) g(t)$  and  $\frac{\partial u_\gamma}{\partial \gamma} = \frac{s}{\gamma^2} \frac{1}{1 - F(u_\gamma)}$ . Thus,

$$\begin{aligned}
\frac{\partial W^*}{\partial t} &= \frac{\partial(\gamma u_\gamma)}{\partial \gamma} \frac{\partial \gamma}{\partial t} - t g(t) \\
&= \left[ \left( u_\gamma + \frac{s}{\gamma} \frac{1}{1 - F(u_\gamma)} \right) (\beta_h - \beta_l) - t \right] g(t).
\end{aligned} \tag{38}$$

Clearly  $\frac{\partial W^*}{\partial t}|_{t=0} > 0$ . Moreover, for given  $s > 0$ ,  $u_\gamma$  is bounded away from  $\bar{u}$ . Thus,  $\frac{\partial W^*}{\partial t} < 0$  if  $t$  is sufficiently high. Hence, there exists  $t^o \in (0, \bar{x})$  such that  $W^*$  is maximized at  $t^o$ . Moreover, from (15),  $t^*$  increases in  $s$  and  $t^* \rightarrow \bar{t}$  if  $s \rightarrow \bar{s}$ . Therefore, if  $t^o < \bar{t}$ , there exists a unique  $\sigma$  such that  $t^* \leq t^o$  when  $s \leq \sigma$ , and  $t^* > t^o$  when  $\sigma < s \leq \bar{s}$ . ■

**Proof of Lemma 1.** In equilibrium, constraint (26) is binding when  $x = t_k$  and thus

$$(1 - \mu) \frac{1}{G(t_k)} \beta_h \lambda(u_h) (1 + \delta) = k + t_k.$$

Hence,

$$\Psi = \beta_h \lambda(u_h) (1 + \delta) - t_k G(t_k),$$

which decreases in  $t_k$ . Thus, the intermediary optimally sets  $(k^*, \tau^*)$  such that the firm with  $x = t_\Omega$  is indifferent between being on and off the platform:

$$k^* = (1 - \mu^*) \frac{1}{G(t_\Omega)} \beta_h \frac{1 - F(u_h)}{f(u_h)} (1 + \delta) - t_\Omega.$$

Moreover, substituting  $k^*$  into constraint (25), we have

$$\mu^* < t_\Omega G(t_\Omega) \frac{1}{\delta \beta_h} \frac{f(u_h)}{1 - F(u_h)}.$$

Therefore,  $\mu^* = 0$  and  $k^*$  solve problem (P1) and induce the separating equilibrium, which improves search efficiency in period 1. If additionally  $t_\Omega \leq t^*$ , then the total investment cost on quality is not higher in the separating equilibrium than in the equilibrium without the intermediary, and hence social welfare must be higher in the former. ■

**Proof of Lemma 2.** Constraint (30) is binding when  $x = t_k$ , with

$$t_k = (1 - \mu) \delta \frac{1}{G(t_k)} \beta_h \lambda(u_h). \quad (39)$$

Since RHS of (39) decreases in  $t_k$  and  $\mu$ , it follows that  $t_k$  decreases in  $\mu$ . In equilibrium, (29) is binding. Moreover, from (39),

$$t_k G(t_k) = (1 - \mu) \delta \beta_h \lambda(u_h).$$

Thus, the intermediary's objective function becomes, for  $\gamma = \gamma(t_k)$ ,

$$\Psi = \gamma(t_k) \lambda(u_\gamma) - t_k G(t_k) + \delta \beta_h \lambda(u_h). \quad (40)$$

Since  $\frac{\partial u_\gamma}{\partial \gamma} = \frac{1}{[1 - F(u_\gamma)]} \frac{s}{\gamma^2}$  and  $\frac{\partial \gamma}{\partial t_k} = (\beta_h - \beta_l) g(t_k)$ , we have

$$\begin{aligned} \frac{\partial \Psi}{\partial t_k} &= \left( \lambda(u_\gamma) + \gamma \lambda'(u_\gamma) \frac{\partial u_\gamma}{\partial \gamma} \right) \frac{\partial \gamma}{\partial t_k} - G(t_k) - t_k g(t_k) \\ &= \left( \lambda(u_\gamma) - \lambda'(u_\gamma) \frac{s}{\gamma} \frac{1}{1 - F(u_\gamma)} \right) (\beta_h - \beta_l) g(t_k) - G(t_k) - t_k g(t_k) \\ &= \left[ \left( \lambda(u_\gamma) - \lambda'(u_\gamma) \frac{s}{\gamma} \frac{1}{1 - F(u_\gamma)} \right) (\beta_h - \beta_l) - t_k \right] g(t_k) - G(t_k). \end{aligned} \quad (41)$$

Since  $\lambda'(u_\gamma) \leq 0$ , we have  $\frac{\partial \Psi}{\partial t_k}|_{t_k \rightarrow 0} > 0$ . Also, under (31),  $\frac{\partial \Psi}{\partial t_k}|_{t_k \rightarrow t^*} < 0$ . Therefore, there exists  $t_k^* < t^*$  that maximizes  $\Psi$ , with  $\mu^* > 0$ . ■

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